

Combined LHC/ILC analysis

-- case of heavy sfermions

Gudrid Moortgat-Pick (CERN)

in coll. with: K. Desch, J. Kalinowski, K. Rolbiecki, W.J. Stirling (hep-ph/ 0607104)

Outline

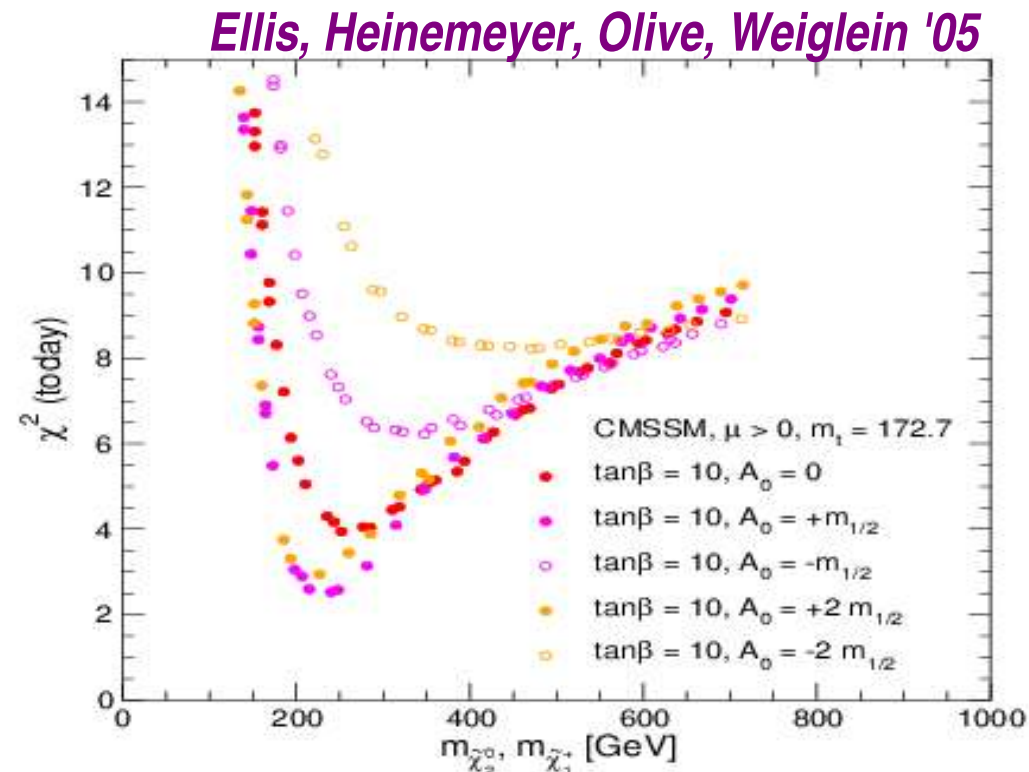
- Introduction: **SUSY parameter determination** and **LHC/ILC interplay**
- Case study: chosen scenario with heavy sfermions
- Numerical results: **expectations for LHC**
- Numerical results: **ILC strategy and LHC/ILC interplay**
- Conclusions

Supersymmetry

- One of the most promising candidates for physics beyond the Standard Model (SM) is Supersymmetry (SUSY)
 - high predictive power, solves hierarchy, unification, dark matter problem etc.
 - every SM particle gets a SUSY partner with the same quantum numbers
 - all these assumptions have to be checked experimentally model-independently!

- In which range do we expect SUSY?

- at least **some light particles** should be accessible at 500 GeV
- **best possible tools** needed to get maximal information out of only the part of the spectrum



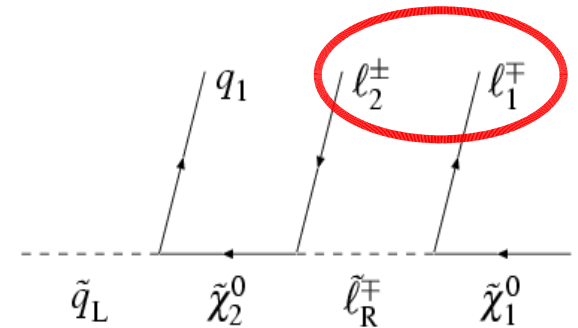
SUSY parameter determination

- **Problem: number of new parameters**
 - **even in the MSSM 105 !**
- **We have only**
 - **constraints** on parameters from **e,n, Hg, etc. dipole moments**
 - **exclusion bounds** from **LEP and Tevatron**
 - **constraints** from low-energy experiments **$b \rightarrow s \gamma, g_{\mu}^{-2}$**
 - **constraints** from **dark matter searches**
- **To reveal the structure of the underlying physics, it is important to determine the parameters in a model-independent way and test all model assumptions experimentally**
- **Soon we will have LHC data, but LHC/ILC interplay will be essential and both machines cover a large range of the parameter space !**

Discovery of SUSY

● Expectations at the LHC:

- Coloured SUSY partners: discovery reach $m_{\tilde{q},\tilde{g}} < 2\text{-}2.5\text{ TeV}$
- Non-coloured partners: a) via Drell-Yan $m_{\tilde{\chi}} < 250\text{ GeV}$
b) via **cascade decay chains**



- Parameter determinations: in specific SUSY breaking models

● At the ILC:

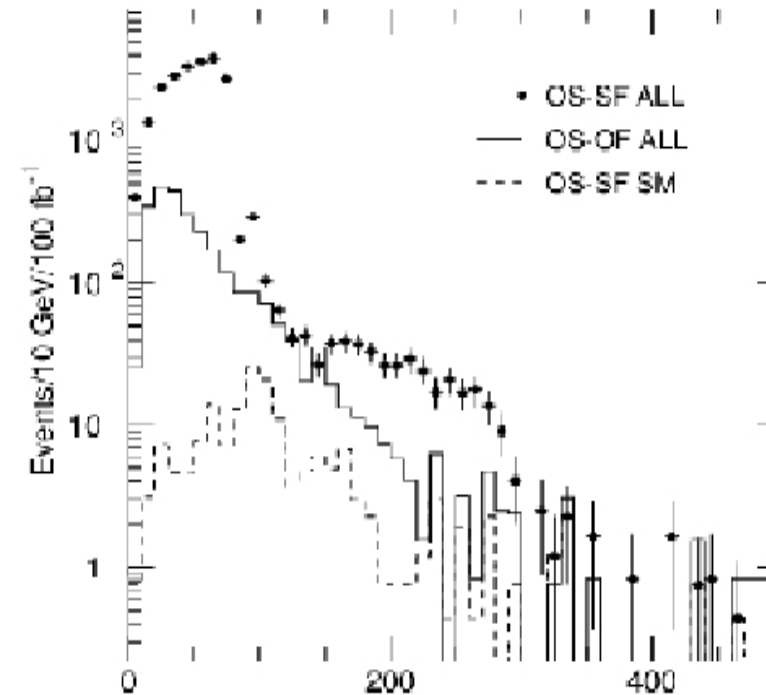
- direct production of all kind of SUSY particles up to kinematical limit $\sqrt{s}/2$
- indirect mass bounds due to high precision
- precise model-independent parameter determination

● Particularly promising field for LHC/ILC interplay studies !

LHC / ILC interplay

- If fundamental parameters determined: allows mass predictions for heavier particles

- significant increase of sensitivity for searches at the LHC and unique identification of particles in decay chain
- powerful test of the model and distinction between e.g. MSSM vs. NMSSM model!



	M_1	M_2	μ	$\tan \beta$
input	99.1	192.7	352.4	10
LC ₅₀₀	99.1 ± 0.2	192.7 ± 0.6	352.8 ± 8.9	10.3 ± 1.5
LHC+LC ₅₀₀	99.1 ± 0.1	192.7 ± 0.3	352.4 ± 2.1	10.2 ± 0.6

- strong improvement in parameter determination via LHC/ILC interplay!

NMSSM versus MSSM

- SUSY scenario in the NMSSM, where Higgs and light particle sector (neutralino / chargino) show no hints for model distinction

- measured at ILC (500 GeV): $m_{\tilde{\chi}_1^\pm}, m_{\tilde{\chi}_{1,2}^0}, \sigma(e^+e^- \rightarrow \tilde{\chi}_1^+ \tilde{\chi}_1^-, \tilde{\chi}_1^0 \tilde{\chi}_2^0)$

→ Consistent within MSSM-analysis:

M1, M2, μ , $\tan\beta$

→ Predictions:

$$m_{\tilde{\chi}_3^0} = [352, 555] \text{ GeV} \rightarrow \text{pure higgsino}$$

$$m_{\tilde{\chi}_4^0} = [386, 573] \text{ GeV} \rightarrow \text{larger gaugino comp.}$$

$$m_{\tilde{\chi}_2^\pm} = [450, 600] \text{ GeV}$$

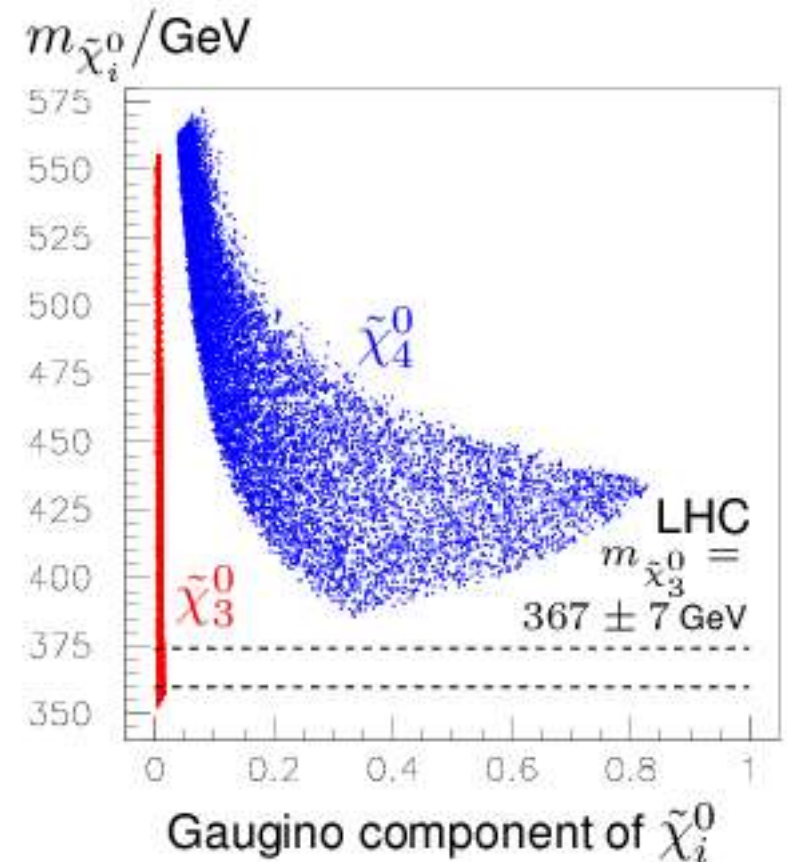
⇒ $\tilde{\chi}_3^0$ not accessible at LHC

- However: $\tilde{\chi}_3^0$ in underlying NMSSM scenario has large gaugino component

→ visible at LHC → inconsistency

- Model inconsistency determined via LHC/ILC**

- motivation for further analysis



Today: heavy sfermions

- **Tricky case: e.g. Split-SUSY or focuspoint - inspired scenarios**
 - features: very heavy squarks, sleptons, heavy H, A but light SM-like h and light gluino and light charginos / neutralinos
 - challenging for the LHC..... but is the ILC in that case the right machine ?
 - some analysis done at LHC, but within mSUGRA and still very difficult

- **Our approach: take a focuspoint-inspired scenario, but do not impose any assumption on the SUSY breaking mechanism and apply LHC / ILC analysis**
 - to impose even more difficult conditions: **only use the ILC(500) !**

- **How well is it possible to**
 - determine the underlying fundamental parameters
 - check some SUSY implications

Chosen scenario

- MSSM parameters:

$$M_1 = 60 \text{ GeV}, M_2 = 121 \text{ GeV}, M_3 = 322 \text{ GeV}, \mu = 540 \text{ GeV}, \tan\beta = 20$$

- Resulting masses:

$m_{\tilde{\chi}_1^\pm}$	$m_{\tilde{\chi}_2^\pm}$	$m_{\tilde{\chi}_1^0}$	$m_{\tilde{\chi}_2^0}$	$m_{\tilde{\chi}_3^0}$	$m_{\tilde{\chi}_4^0}$	$m_{\tilde{g}}$
117	552	59	117	545	550	416

m_h	$m_{H,A}$	m_{H^\pm}
119	1934	1935

→ light gauginos/higgsinos, light gluino, light h but heavy H's, A

$m_{\tilde{\nu}}$	$m_{\tilde{e}_R}$	$m_{\tilde{e}_L}$	$m_{\tilde{\tau}_1}$	$m_{\tilde{\tau}_2}$	$m_{\tilde{q}_R}$	$m_{\tilde{q}_L}$	$m_{\tilde{t}_1}$	$m_{\tilde{t}_2}$
1994	1996	1998	1930	1963	2002	2008	1093	1584

→ heavy squarks and sleptons in the multi-TeV range

What is expected that LHC could do ?

- In principle: all squarks should be kinematically accessible

- stops: $BR(\tilde{t}_{1,2} \rightarrow \tilde{g}t) \sim 66\%$,

- background from t large, no new interesting channels open in decays

- other quarks: decay mainly via gluino and q, but reconstruction of heavy squarks at 2 TeV difficult

- assume: mass resolution of squarks with about 50 GeV
(but that's not important for our further procedure)

- Production of light gluino: perfect for LHC

- excellent for LHC: high rates and interesting decays

Mode	$\tilde{g} \rightarrow \tilde{\chi}_2^0 b\bar{b}$	$\tilde{g} \rightarrow \tilde{\chi}_1^- q_u \bar{q}_d$	$\tilde{\chi}_1^+ \rightarrow \tilde{\chi}_1^0 \bar{q}_d q_u$	$\tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0 \ell^+ \ell^-$	$\tilde{t}_{1,2} \rightarrow \tilde{g}t$	$\tilde{\chi}_1^- \rightarrow \tilde{\chi}_1^0 \ell^- \bar{\nu}_\ell$
BR	14.4%	10.8%	33.5%	3.0%	66%	11.0%

- dilepton edge clearly visible:

$$\delta(m_{\tilde{\chi}_2^0} - m_{\tilde{\chi}_1^0}) \sim 0.5 \text{ GeV}$$

What is expected at the ILC (500) ?

- Kinematically only two light neutralinos and light chargino accessible
 - in reality: neutralino production below 1 fb not impossible, but not used today
 - only chargino production has high rates !
 - subsequent decays: $\tilde{\chi}_1^- \rightarrow \tilde{\chi}_1^0 e^- \bar{\nu}_e, \tilde{\chi}_1^0 \mu^- \bar{\nu}_\mu, \tilde{\chi}_1^0 d \bar{u}, \tilde{\chi}_1^0 s \bar{c}$
- Due to very limited information, use two energies and polarized beams!

\sqrt{s}/GeV	(P_{e^-}, P_{e^+})	$\sigma(\tilde{\chi}_1^+ \tilde{\chi}_1^-)/\text{fb}$	$\sigma(\tilde{\chi}_1^+ \tilde{\chi}_1^-) B_{slc} e_{slc}/\text{fb}$
350	(-90%, +60%)	6195.5	1062.5 ± 4.0
	(+90%, -60%)	85.0	14.6 ± 0.7
500	(-90%, +60%)	3041.5	521.6 ± 2.3
	(+90%, -60%)	40.3	6.9 ± 0.4

- uncertainties: efficiency 50%, 1σ stat. uncertainties, $\Delta P / P = 0.5\%$
- background WW: in semileptonic mass constraints applicable

Mass measurements at LHC+ILC

Expected chargino mass resolution:

→ in the continuum: up to 0.5 GeV

→ threshold scan:

$$m_{\tilde{\chi}_1^\pm} = 117.1 \pm 0.1 \text{ GeV}$$

Neutralino mass resolution:

→ use either energy $\tilde{\chi}_1^- \rightarrow \tilde{\chi}_1^0 \ell^- \bar{\nu}_\ell$ or invariant mass distribution $\tilde{\chi}_1^- \rightarrow \tilde{\chi}_1^0 q d \bar{q}_u$

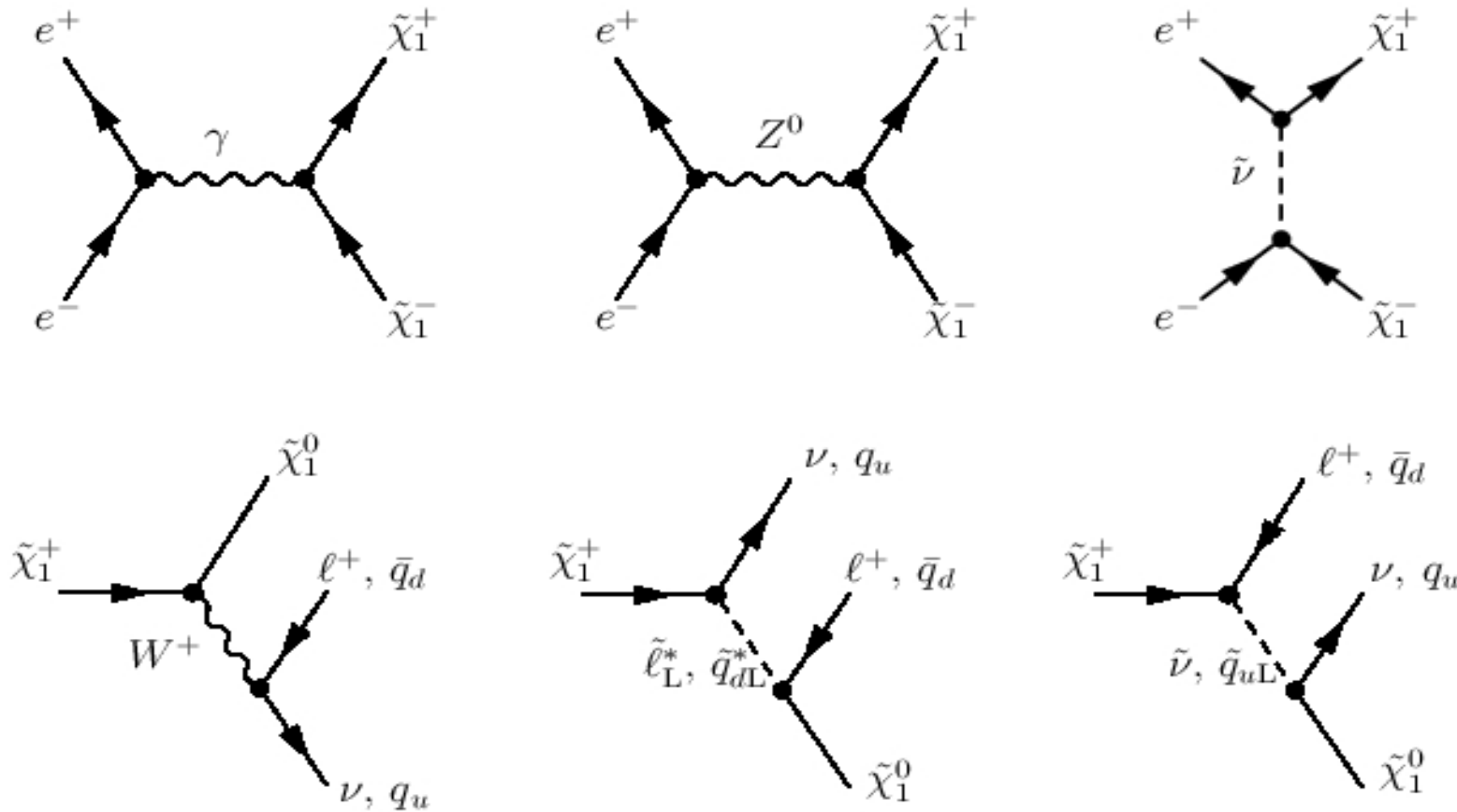
$$m_{\tilde{\chi}_1^0} = 59.2 \pm 0.2 \text{ GeV}$$

→ together with LHC mass information ($\delta(m_{\tilde{\chi}_2^0} - m_{\tilde{\chi}_1^0}) \sim 0.5 \text{ GeV}$):

$$m_{\tilde{\chi}_2^0} = 117.1 \pm 0.5 \text{ GeV}$$

Strategy to determine fundamental parameters

- On which parameters depend the process?



→ Parameters in the gaugino/higgsino: $M_1, M_2, \mu, \tan \beta$

→ But heavy virtual particles: $m_{\tilde{\nu}}, m_{\tilde{\ell}}, m_{\tilde{q}_L}, m_{\tilde{q}_R}$

Strategy, 1st step

- Use measured masses and polarized cross sections
- Convert them analytically and derive / fit the parameters within uncertainties
 - ⇒ do χ^2 test for M_1 , M_2 , μ and $m_{\tilde{\nu}}$
 - ⇒ BR not sensitive to heavy slepton masses
 - ⇒ was necessary to fix $\tan\beta$ (took several values) to get convergence of fit !
- Results:
 - ⇒ contradiction to theory for $\tan\beta < 1.7$
 - ⇒
$$59.4 \leq M_1 \leq 62.2 \text{ GeV}, \quad 118.7 \leq M_2 \leq 127.5 \text{ GeV},$$
$$450 \leq \mu \leq 750 \text{ GeV}, \quad 1800 \leq m_{\tilde{\nu}_e} \leq 2210 \text{ GeV}$$
 - ⇒ M_1 , M_2 good (~5%), but μ and $m_{\tilde{\nu}}$ rather weak (~16%) due to limited information

Strategy, 2nd step -- intro spin correlations

- Which further observable could be used?

→ **Forward-backward asymmetry of the final lepton / quark**

(angle between incoming beam and final lepton or quark)

- Strongly dependent on spin correlations of decaying chargino:

→ **amplitude squared:** $e^- + e^+ \rightarrow \tilde{\chi}_1^+ + \tilde{\chi}_1^-$ and $\tilde{\chi}_1^- \rightarrow \tilde{\chi}_1^0 + \ell^- + \bar{\nu}$

$$|T|^2 = |\Delta_{f_1}|^2 |\Delta_{f_2}|^2 \sum_{fin.sp.} \overbrace{(P^{\lambda_{f_1} \lambda_{f_2}} P^{*\lambda'_{f_1} \lambda'_{f_2}})}^{\text{spin-density matrix}} \times \overbrace{(Z_{\lambda_{f_1}} Z_{\lambda'_{f_1}}^*)}^{\text{decay matrix}} \times \overbrace{(Z_{\lambda_{f_2}} Z_{\lambda'_{f_2}}^*)}^{\text{decay matrix}}$$

$$\longrightarrow |T|^2 \sim PD_i D_j + \sum_a^P \sum_a^D D_j + \sum_b^P \sum_b^D D_i + \sum_{ab}^P \sum_a^D \sum_b^D$$

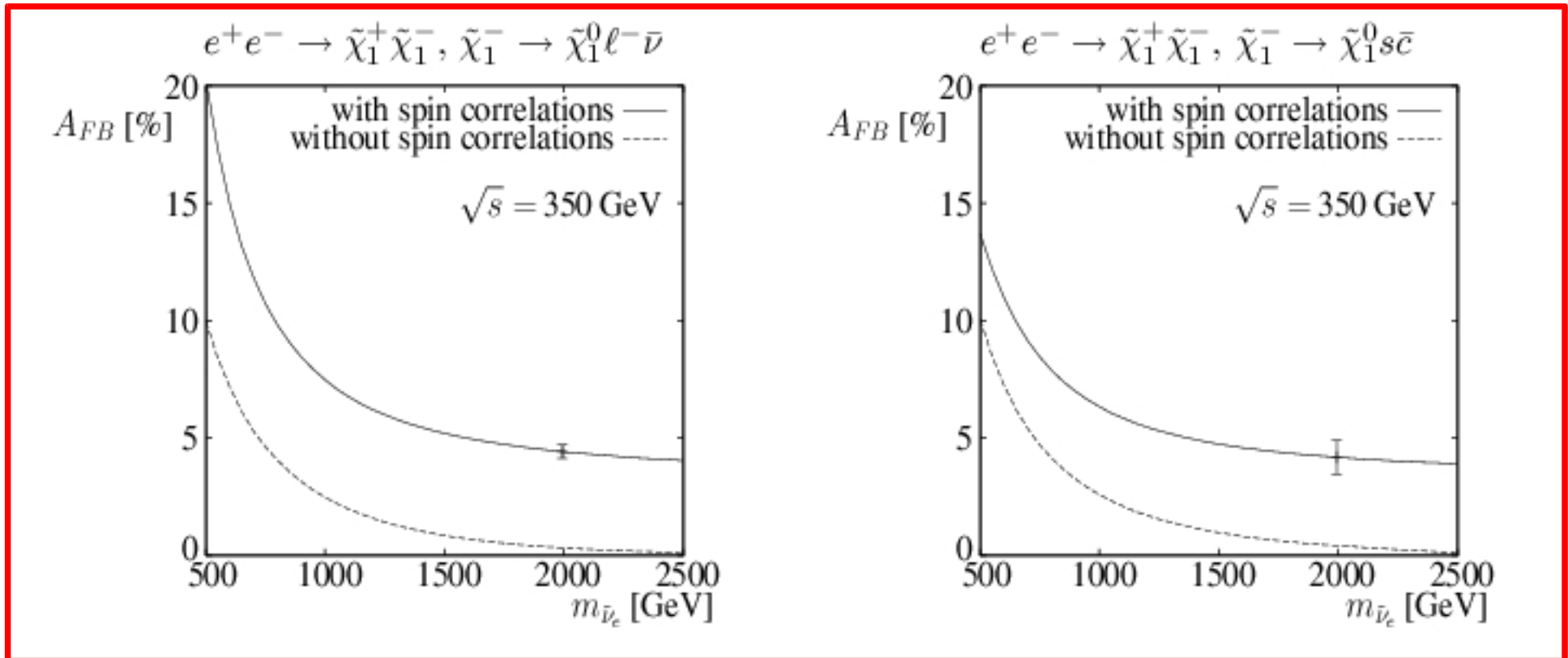
↓
↓
↓
↓

cross section
A_{fb}(I⁻)
A_{fb}(I⁺)
not needed here

'new
contributions'

How important are spin correlations?

● Impact of the 'new contributions' on A_{fb} :



- strong influence of spin correlations: A_{fb} within [5%, 20%]
- still sensitivity to heavy sneutrino mass !

Strategy, 2nd step -- with leptonic A_{fb}

- use measured masses, cross sections and leptonic A_{fb}
- since decay also depends on unknown left slepton mass, use SU(2) relation:

$$m_{\tilde{e}_L}^2 = m_{\tilde{\nu}_e}^2 + m_Z^2 \cos(2\beta)(-1 + \sin^2 \theta_W)$$

- include also statistical and polarization uncertainty for A_{fb} :

\sqrt{s}/GeV	(P_{e^-}, P_{e^+})	$A_{\text{FB}}(\ell^-)/\%$	$A_{\text{FB}}(\bar{c})/\%$
350	$(-90\%, +60\%)$	4.42 ± 0.29	4.18 ± 0.74
	$(+90\%, -60\%)$	–	–
500	$(-90\%, +60\%)$	4.62 ± 0.41	4.48 ± 1.05
	$(+90\%, -60\%)$	–	–

- use only (- +) values due to statistical uncertainty

Strategy, 2nd step -- results

● Results:

→ do χ^2 test for M_1 , M_2 , μ , m_ν and $\tan\beta$

→ not necessary to fix $\tan\beta$

$$\begin{aligned} 59.7 \leq M_1 \leq 60.35 \text{ GeV}, & \quad 119.9 \leq M_2 \leq 122.0 \text{ GeV}, \\ 500 \leq \mu \leq 610 \text{ GeV}, & \quad 14 \leq \tan\beta \leq 31 \\ 1900 \leq m_{\tilde{\nu}_e} \leq 2100 \text{ GeV} \end{aligned}$$

● Improvements:

→ prediction of **sneutrino mass by factor 2**

→ accuracy of **M_1 , M_2 by factor 5**

→ accuracy of **μ by factor 1.6** and **$\tan\beta$ now included!**

Strategy, 3rd step -- also hadronic A_{fb}

- Include also A_{fb} from hadronic distribution:

- no SU(2) assumption necessary, since squark masses known from LHC!
- charm identification needed : assume c-tag efficiency of 40% for selection efficiency of 50%

- Results:

$$59.45 \leq M_1 \leq 60.80 \text{ GeV}, \quad 118.6 \leq M_2 \leq 124.2 \text{ GeV}, \quad 420 \leq \mu \leq 770 \text{ GeV}$$
$$1900 \leq m_{\tilde{\nu}_e} \leq 2120 \text{ GeV}, \quad m_{\tilde{e}_L} \geq 1500 \text{ GeV}, \quad 11 \leq \tan \beta \leq 60.$$

- most significant improvement: factor 2 for sneutrino mass prediction
- no upper bound for selectron mass, but consistent with SU(2) relation

Conclusions

- **Angular distributions very powerful observables**
 - contain 'new' contributions (the spin correlations)
- **With forward-backward asymmetries sensitive to heavy virtual particles**
 - even in multi-TeV range far beyond kinematical limit
 - rather accurate parameter determination possible
 - possible even in challenging scenarios !
 - high model-independence
- **LHC / ILC interplay crucial**
 - further examples coming up

Do not be afraid for heavy sleptons and squarks at LHC and ILC (500) !